

Particle Dynamic Simulation

Principal Issues

- Packing fraction and flow control through exposed region (bridging, acceleration)
- Particle ejection (scattering)
- Multi-zone flows (mixing, shear flows)
- Heat transfer
- Heat exchanger optimization

Particle Dynamic Simulation

Computational Tools

- During the past few years, direct simulation models have become available for solving the momentum equations for large assemblies of particles
- The **PFC2D** code was used for simulating the flow in APPLE:
 - * 2D cylinders (or 3D spheres in PFC3D)
 - * ability to define individual pebbles or create large assemblies with a single command
 - * memory-efficient explicit solution
16 MB ram corresponds with 40,000 particles
 - * runs on a PC
- These models have been tested and applied to a wide variety of applications in soil mechanics, seismic response, mechanics of materials and material mixing.
- Heat transfer is not included, but can be incorporated using pebble positions, rotations, and contact information from PFC.

PFC Code Description

Particle Simulation:

- All particles are circular (but can be clumped into complex shapes)
- Particles are treated as rigid bodies
- Contact occurs at a point
- A soft-contact approach allows particles to overlap at contacts
- The magnitude of overlap is related to the contact force
via force-displacement law

Contact Models:

- Linear or Hertz contact
- Static and sliding friction
- Finite normal and shear stiffness
- Bonding forces

Numerical Approach

- Distinct Element Method (DEM)*
- Translation and rotation included
- Time step is optimized from stiffness matrix, $m\ddot{x} + kx = 0$
$$\tau_{crit} = \sqrt{m/k}$$
- Dissipation by frictional sliding, non-viscous damping can be applied to Equations of Motion for optimal static convergence

* P. A. Cundall, *Int. J. Rock Mechanics, Mineral Science and Geomechanics Abstracts*, 1988.

Calculation Cycle in PFC

1. Update particle and wall positions and velocities
update set of contacts

4. Apply law of motion
(to each particle)
using forces and moments

2. Apply force-displacement law
(to each contact)
using relative motions and
constitutive laws

3. Update contacts forces

Example Problem: Flow from a Vertical Chute

Wall Geometry:

10-cm chute width	
upper compaction zone	35 cm
guided flow zone	15 cm
free-fall zone	50 cm
friction coefficient = 0.2	

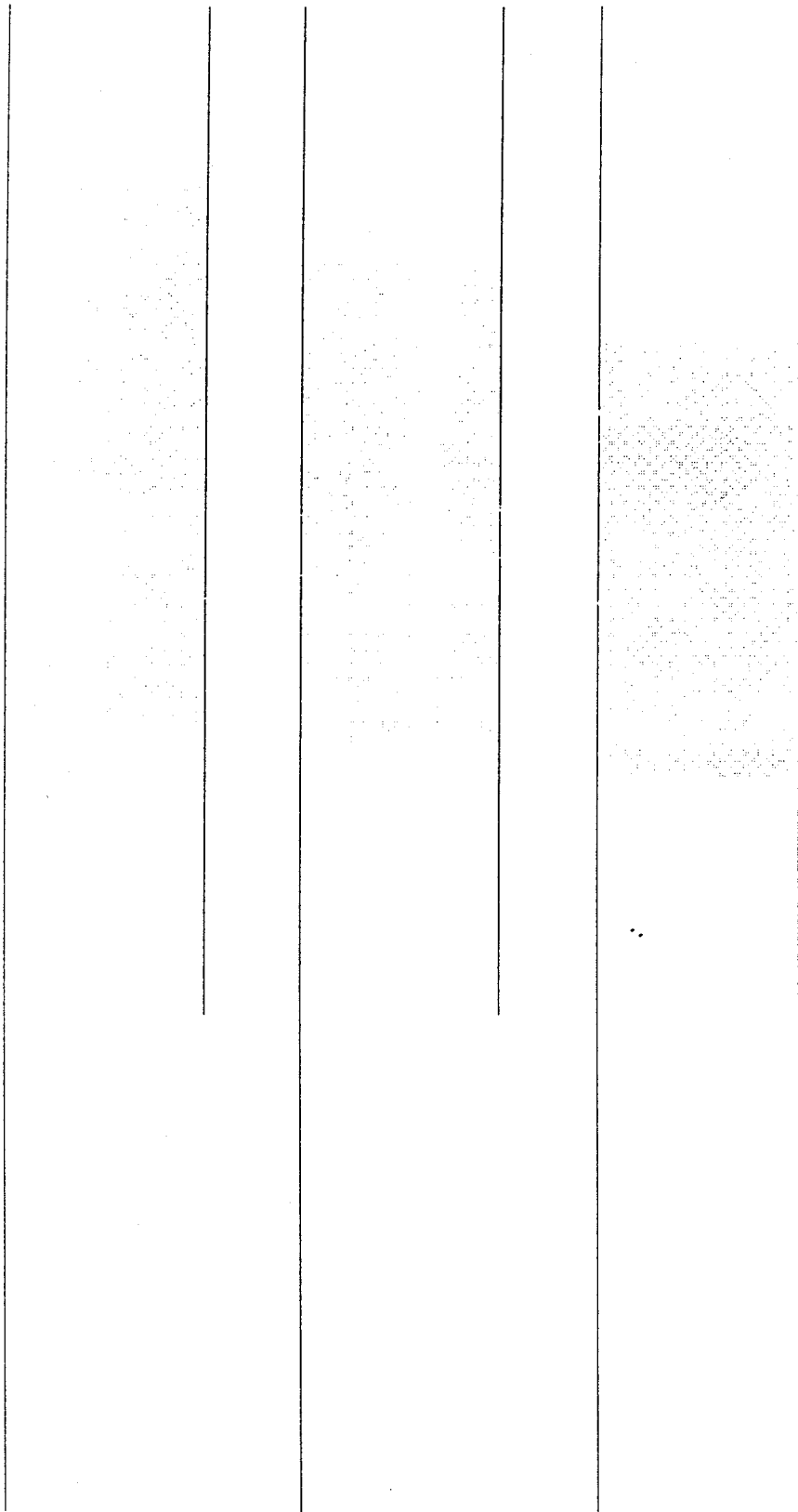
Pebble Properties:

10,000 spheres
1-mm uniform diameter
friction coefficient = 0.5
density = 2000 kg/m^3
linear force-displacement, $k=10^6 \text{ N/m}$

Time Sequence:

1. dispersely fill upper zone (0.65–1.0 m)
2. partial compaction for 2 s
3. remove wall at $z=0.65$
4. track pebble dynamics for 5 s

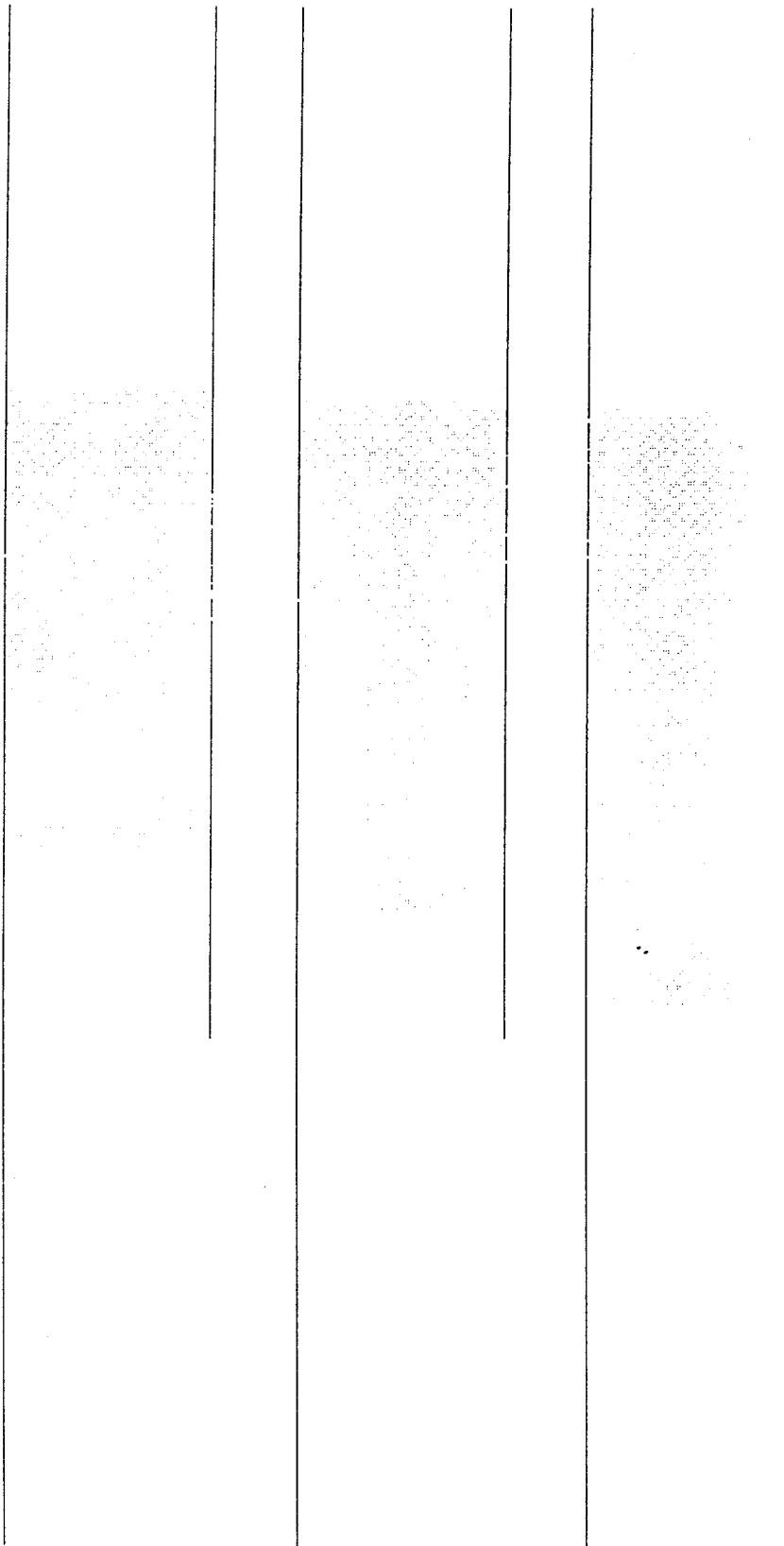
Bed Geometry and Forces, $t=0.5-1.5$ sec.



Observations

1. No observed tendency for particles to be ejected
Low packing fraction, Low shear observed
2. Tight packing is difficult to maintain in the free-fall zone
Intenal forces are important in free-fall, even with $L/r \geq 10$
3. Need to explore baffle arrangements and/or curved walls
4. The code is very easy to use – scoping of new geometries and multi-layer flows will be done in the near future
5. Addition of heat transfer will be a major undertaking
 - contact conduction
 - radiation transport

Bed Geometry and Forces, $t=2.0-3.0$ sec.



Bed Geometry and Forces, $t=3.5-4.5$ sec.

